Wednesday, January 21

Example: The "data frame" `trees` comes with R. We can see it if we just type `trees` at the prompt in the R console.

```
trees
```

```
   Girth Height Volume
1    8.3     70   10.3
2    8.6     65   10.3
3    8.8     63   10.2
4   10.5     72   16.4
5   10.7     81   18.8
6   10.8     83   19.7
7   11.0     66   15.6
8   11.0     75   18.2
9   11.1     80   22.6
10  11.2     75   19.9
11  11.3     79   24.2
12  11.4     76   21.0
13  11.4     76   21.4
14  11.7     69   21.3
15  12.0     75   19.1
16  12.9     74   22.2
17  12.9     85   33.8
18  13.3     86   27.4
19  13.7     71   25.7
20  13.8     64   24.9
21  14.0     78   34.5
22  14.2     80   31.7
23  14.5     74   36.3
24  16.0     72   38.3
25  16.3     77   42.6
26  17.3     81   55.4
27  17.5     82   55.7
28  17.9     80   58.3
29  18.0     80   51.5
30  18.0     80   51.0
31  20.6     87   77.0
```

Note that with R a "data frame" is a particular kind of object that is frequently used to store data.

Let's specify the model

$$E(V_i) = \beta_0 + \beta_1 g_i + \beta_2 h_i,$$

where V_i, g_i, and h_i are the volume, girth, and height from the i-th observation.

```
m <- lm(formula = Volume ~ Girth + Height, data = trees)
```

There's a lot to say here.

1. `lm` (**l**inear **m**odel) is a *function* to which we have provided two *arguments*: `formula` and `data`. Other arguments can be found using `args(lm)`, some of which we will use later.

```
args(lm)
```

```
function (formula, data, subset, weights, na.action, method = "qr",
    model = TRUE, x = FALSE, y = FALSE, qr = TRUE, singular.ok = TRUE,
    contrasts = NULL, offset, ...)
NULL
```

   We do not need to name the arguments *if we provide them in the same order as they are expected*. For example, this would also work:

```
m <- lm(Volume ~ Girth + Height, trees)
```

   Just about all functions that estimate a regression model expect `formula` to be the first argument. A common convention (and one that I use) is to name all arguments except the first:

```
m <- lm(Volume ~ Girth + Height, data = trees)
```

2. The `formula` argument is *symbolic*, not literal. It is a system for communicating with R the regression model you want to specify. The model formula `Volume ~ Girth + Height` implies the statistical model $E(V_i) = \beta_0 + \beta_1 g_i + \beta_2 h_i$.

3. We have *assigned* the output of this function to an *object* called `m` (R is an *object-oriented* programming language). Note that you can also use `=` instead of `<-`. We can apply other functions to this object. For example, `print(m)`.

```
print(m)
```

```

Call:
lm(formula = Volume ~ Girth + Height, data = trees)

Coefficients:
(Intercept)        Girth       Height
   -57.9877       4.7082       0.3393
```

   But if you just have `m` it will interpret that as `print(m)`.

```
m
```

```

Call:
lm(formula = Volume ~ Girth + Height, data = trees)

Coefficients:
(Intercept)        Girth       Height
   -57.9877       4.7082       0.3393
```

   A bit more information can be extracted by using the `summary` function.

```
summary(m)
```

```

Call:
lm(formula = Volume ~ Girth + Height, data = trees)

Residuals:
    Min      1Q  Median      3Q     Max
-6.4065 -2.6493 -0.2876  2.2003  8.4847
```

```
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -57.9877     8.6382  -6.713 2.75e-07 ***
Girth         4.7082     0.2643  17.816  < 2e-16 ***
Height        0.3393     0.1302   2.607   0.0145 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 3.882 on 28 degrees of freedom
Multiple R-squared:  0.948,   Adjusted R-squared:  0.9442
F-statistic:   255 on 2 and 28 DF,  p-value: < 2.2e-16
```

In lecture I will often trim the output from `summary` using something like the following.

```
summary(m)$coefficients
```

```
               Estimate Std. Error   t value     Pr(>|t|)
(Intercept) -57.9876589  8.6382259 -6.712913 2.749507e-07
Girth         4.7081605  0.2642646 17.816084 8.223304e-17
Height        0.3392512  0.1301512  2.606594 1.449097e-02
```

This shows estimates of the parameters β_0, β_1, and β_2, and some other information concerning inferences for those parameters (more on that later).

Example: Here are the data and a specified linear model for the study on dopamine activity in schizophrenics. The data are available in the **BSDA** package.

```
library(BSDA) # install with install.packages("BSDA")
Dopamine
```

```
# A tibble: 25 x 2
     dbh group
   <int> <chr>
 1   104 nonpsychotic
 2   105 nonpsychotic
 3   112 nonpsychotic
 4   116 nonpsychotic
 5   130 nonpsychotic
 6   145 nonpsychotic
 7   154 nonpsychotic
 8   156 nonpsychotic
 9   170 nonpsychotic
10   180 nonpsychotic
# i 15 more rows
```

```
head(Dopamine)
```

```
# A tibble: 6 x 2
    dbh group
  <int> <chr>
1   104 nonpsychotic
2   105 nonpsychotic
3   112 nonpsychotic
4   116 nonpsychotic
5   130 nonpsychotic
6   145 nonpsychotic
```

```
tail(Dopamine)
```

```
# A tibble: 6 x 2
    dbh group
  <int> <chr>
1   226 psychotic
2   245 psychotic
3   270 psychotic
4   275 psychotic
5   306 psychotic
6   320 psychotic
```

Also you can try `?Dopamine` or `help(Dopamine)` to see the help file (you can also do this for functions like `lm`). A `tibble` is another way that data are stored in R that is mostly interchangeable with data frames (they are effectively "enhanced" data frames).

Let's specify a linear model using the `lm` function.

```
m <- lm(dbh ~ group, data = Dopamine)
summary(m)$coefficients
```

```
                Estimate Std. Error   t value     Pr(>|t|)
(Intercept)    164.26667   12.58563 13.051923 4.058662e-12
grouppsychotic  78.33333   19.89963  3.936422 6.586761e-04
```

Note: The `grouppsychotic` tells us that an indicator variable was created for the level/category `psychotic` for the categorical variable `group`. How would we write this model *mathematically*?

Example: Here are the data from the anorexia study.

```
library(MASS) # install with install.packages("MASS")
head(anorexia)
```

```
  Treat Prewt Postwt
1  Cont  80.7   80.2
2  Cont  89.4   80.1
3  Cont  91.8   86.4
4  Cont  74.0   86.3
5  Cont  78.1   76.1
```

```
6  Cont  88.3   78.1
```

```
summary(anorexia)
```

```
  Treat        Prewt           Postwt
 CBT :29   Min.   :70.00   Min.   : 71.30
 Cont:26   1st Qu.:79.60   1st Qu.: 79.33
 FT  :17   Median :82.30   Median : 84.05
           Mean   :82.41   Mean   : 85.17
           3rd Qu.:86.00   3rd Qu.: 91.55
           Max.   :94.90   Max.   :103.60
```

Here we are going to create another variable `change` which is the change in weight. (Note: I redefined `change` from the original lecture as the post-weight minus the pre-weight so that a positive value indicates weight gain and a negative value indicates weight loss.)

```
anorexia$change <- anorexia$Postwt - anorexia$Prewt
head(anorexia)
```

```
  Treat Prewt Postwt change
1  Cont  80.7   80.2   -0.5
2  Cont  89.4   80.1   -9.3
3  Cont  91.8   86.4   -5.4
4  Cont  74.0   86.3   12.3
5  Cont  78.1   76.1   -2.0
6  Cont  88.3   78.1  -10.2
```

Let's specify a linear model.

```
m <- lm(change ~ Treat, data = anorexia)
summary(m)$coefficients
```

```
             Estimate Std. Error   t value   Pr(>|t|)
(Intercept)  3.006897   1.397996  2.150861 0.03499197
TreatCont   -3.456897   2.033297 -1.700144 0.09360765
TreatFT      4.257809   2.299644  1.851508 0.06837576
```

What are the indicator variables? How would we write this model mathematically?

We can change the parameterization using `relevel`.

```
anorexia$Treat <- relevel(anorexia$Treat, ref = "Cont")
m <- lm(change ~ Treat, data = anorexia)
summary(m)$coefficients
```

```
             Estimate Std. Error    t value    Pr(>|t|)
(Intercept) -0.450000   1.476449 -0.3047854 0.761447048
```

```
TreatCBT     3.456897   2.033297  1.7001438 0.093607652
TreatFT      7.714706   2.348163  3.2854224 0.001602338
```

What are the indicator variables? How would we write this model mathematically?

Note: We can change the parameterization for the model for the previous example, but we need to make `group` a *factor* because the `relevel` function will only work on variables that are factors (although the function `lm` automatically converts a character variable to a factor). We can see that it is not a factor (yet) from `summary` and also from the `is.factor` function.

```
summary(Dopamine)
```

```
      dbh           group
 Min.   :104.0   Length:25
 1st Qu.:150.0   Class :character
 Median :200.0   Mode  :character
 Mean   :195.6
 3rd Qu.:230.0
 Max.   :320.0
```

```
is.factor(Dopamine$group)
```

```
[1] FALSE
```

Here's what happens if you try to use `relevel` with the `group` variable.

```
Dopamine$group <- relevel(Dopamine$group, ref = "psychotic")
```

```
Error in `relevel.default()`:
! 'relevel' only for (unordered) factors
```

Let's make `group` a factor and then change the parameterization.

```
Dopamine$group <- factor(Dopamine$group)
Dopamine$group <- relevel(Dopamine$group, ref = "psychotic")
```

Note that we could also have done this with one line of code.

```
Dopamine$group <- relevel(factor(Dopamine$group), ref = "psychotic")
```

Here's the reparameterized model.

```
m <- lm(dbh ~ group, data = Dopamine)
summary(m)$coefficients
```

```
                  Estimate Std. Error   t value     Pr(>|t|)
(Intercept)       242.60000   15.41419 15.738750 8.320341e-14
groupnonpsychotic -78.33333   19.89963 -3.936422 6.586761e-04
```

What is this model?

Here's another parameterization. Including the term `0` or `-1` in the model formula argument suppresses the inclusion of the β_0 parameter (again, it is symbolic, not literal).[1]

```
m <- lm(dbh ~ 0 + group, data = Dopamine)
summary(m)$coefficients
```

```
                  Estimate Std. Error  t value     Pr(>|t|)
grouppsychotic    242.6000   15.41419 15.73875 8.320341e-14
groupnonpsychotic 164.2667   12.58563 13.05192 4.058662e-12
```

Let's try that with the `anorexia` data.

```
m <- lm(change ~ 0 + Treat, data = anorexia)
summary(m)$coefficients
```

```
           Estimate Std. Error    t value     Pr(>|t|)
TreatCont -0.450000   1.476449 -0.3047854 0.7614470484
TreatCBT   3.006897   1.397996  2.1508614 0.0349919664
TreatFT    7.264706   1.825915  3.9786656 0.0001687833
```

What are these models?

Example: Sometimes we may also want so basic descriptive statistics. There are *many* ways to do this in R. One flexible approach is to use the **dplyr** package.

```
library(dplyr) # install with install.packages("dplyr") or install.packages("tidyverse")
Dopamine |> group_by(group) |> summarize(dbh = mean(dbh))
```

```
# A tibble: 2 x 2
```

[1] When we say something like `dbh ~ group` this is actually translated as `dbh ~ 1 + group` where the "explanatory variable" of `1` effectively becomes the term β_0. Including this term is the default even if we do not mention it explicitly. But if we do not want it then we "add" `0` or `-1` to the model formula to remove it.

```
  group          dbh
  <fct>        <dbl>
1 psychotic     243.
2 nonpsychotic  164.
```

```
anorexia |> mutate(change = Prewt - Postwt) |> group_by(Treat) |>
  summarize(meanchange = mean(change), sdchange = sd(change), samplesize = n())
```

```
# A tibble: 3 x 4
  Treat meanchange sdchange samplesize
  <fct>      <dbl>    <dbl>      <int>
1 Cont       0.450     7.99         26
2 CBT       -3.01      7.31         29
3 FT        -7.26      7.16         17
```

We could have used `mutate` to create the variable `change` for our analysis above.

```
anorexia <- anorexia |> mutate(change = Prewt - Postwt)
m <- lm(change ~ Treat, data = anorexia)
summary(m)$coefficients
```

```
             Estimate Std. Error    t value    Pr(>|t|)
(Intercept)  0.450000   1.476449  0.3047854 0.761447048
TreatCBT    -3.456897   2.033297 -1.7001438 0.093607652
TreatFT     -7.714706   2.348163 -3.2854224 0.001602338
```

The **dplyr** and **tidyr** packages are very useful for manipulating and summarizing data. They have a bit of a learning curve, but they are well worth learning. I will provide many examples of how they can be used.